

CAPACITOR

$$Q = CV \quad \left[\frac{C}{\text{Volt}} = \text{farad} \right]$$

- Depends on size, shape and medium b/w them
- Slope of Q/V graph
- Dimension - $[M^{-1}L^{-2}T^4A^2]$
- 2 spherical capacitor :-

$$C = \frac{QR}{KQ} = 4\pi\epsilon_0 R$$

special case :-

$$\begin{array}{ccc} \text{---} & \rightarrow & \bigcirc \\ \text{---} & & \end{array} \quad Q = nq$$

$$C' = n^{1/3}C \quad U' = n^{5/3}U$$

$$V' = n^{2/3}V \quad R = n^{1/3}R$$

- Combination of spherical capacitor :-

$$C = 4\pi\epsilon_0 \left[\frac{ab}{a-b} \right]$$

$b = \infty$
 $C = 4\pi\epsilon_0 a$

Parallel Plate Capacitor :-

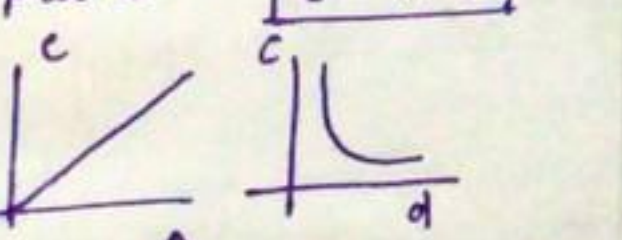
$$E_{\text{net}} = \frac{\sigma}{\epsilon_0} = \frac{Q}{A\epsilon_0}$$

$$\Delta V = \frac{\sigma d}{\epsilon_0} = \frac{Qd}{A\epsilon_0}$$

$$E (\text{due to plate}) = \frac{\sigma}{2\epsilon_0} = \frac{Q}{2A\epsilon_0}$$

$$C_0 = \frac{Q}{\Delta V} = \frac{A\epsilon_0}{d} \quad C' = K \frac{A\epsilon_0}{d}$$

Dielectric induced b/w plates :- $C' = KC_0$



- Force b/w the plates :-

$$F = \frac{Q^2}{2A\epsilon_0} = \frac{\sigma^2 A}{2\epsilon_0} \quad F = qE$$

- Pressure on the plates :-

$$P = \frac{Q^2}{2A^2\epsilon_0} = \frac{\sigma^2}{2\epsilon_0} \quad \leftarrow \text{same as energy density}$$

- Energy density :-

$$E = \frac{\sigma^2}{2\epsilon_0} = \frac{Q^2}{2\epsilon_0 A^2}$$

Total Energy stored

• Energy on capacitor :-

$$E = \frac{1}{2} CV^2 = \frac{1}{2} \frac{Q^2}{C} = \frac{1}{2} QV$$

$$V_A - V_B = Q/C \quad \text{+ase - a jayega to - Q/C karega}$$

• self energy :- for spherical capacitor =

$$U = \frac{Q^2}{8\pi\epsilon_0 R} \quad u = \left(\frac{KQ^2}{2R} \right)$$

• Cylindrical capacitor :- $C = \frac{2\pi\epsilon_0 L}{\log_e(b/a)}$

charging of capacitor :-

• WD by battery in charging capacitor = CV^2

• WD in charging capacitor = $\frac{1}{2} CV^2$

• $U_{\text{loss}} = \frac{1}{2} CV^2$ (Heat)

• MR* for calculating loss :-

$$U_i + W_{\text{battery}} = U_f + U_{\text{loss}}$$

$$\frac{1}{2} CV_i^2 + Q\Delta V = \frac{1}{2} CV_f^2$$

→ Connection of 2 capacitor :-

- Same terminal connection

$$V_c = \frac{C_1 V_1 + C_2 V_2}{C_1 + C_2} = \frac{q_1 + q_2}{C_1 + C_2}$$

Loss in Energy $\Delta U = \frac{1}{2} \frac{C_1 C_2 (V_1 - V_2)^2}{C_1 + C_2}$

Final charge $q_f' = C_1 V_c$
 $q_2' = C_2 V_c$
Transfer = $[q - q_f']$

- Reverse polarity connection :-

$$V_c = \frac{C_1 V_1 - C_2 V_2}{C_1 + C_2} \quad \Delta U = \frac{1}{2} \frac{C_1 C_2 (V_1 + V_2)^2}{C_1 + C_2}$$

$$V_c = \frac{V}{1+K} \quad \rightarrow \text{1 Air capacitor with other filled with dielectric}$$

Combination of capacitor :-

- Series :- $Q = \text{same}$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} + \dots \quad C \propto \frac{1}{V}$$

Jisme C ↑ usme V ↓

- Parallel :- $V = \text{same}$

$$C_{eq} = C_1 + C_2 + \dots \quad q \propto C$$

Jisme C ↑ uska q ↑

- If n-identical connected in series and parallel :-

1) series $C_{eq} = \frac{C}{n}$

2) parallel $C_{eq} = nC$

C_{eq} is smaller than the smallest C C_{eq} is larger than the largest C.

• Breakdown Voltage :-

V_{max} that can be applied across a C.

• series - $V_B = V_1 + V_2 + V_3 + \dots$

• Parallel - $V_B = V$ Special case

$$\frac{A}{B} \propto \frac{C}{C}$$

No. of gap = No. of C

• Wheatstone :- $\frac{C_1}{C_4} = \frac{C_2}{C_3}$

• Cube capacitance :-

(side) $C_{AB} = \frac{12}{7}$, (face) $C_{AC} = \frac{4}{3}$, (body) $C_{AD} = \frac{6}{5}$

★ Dielectric Medium in an External Electric field :-

$$E_{\text{net}} = \frac{E_0}{K}$$

Jaise Coulomb F ↓ 'K' times, similarly E field ↓ 'K' times.

A) SERIES COMBINATION :-

1 ke bad 1 datte hai.

$$C = \frac{A\epsilon_0}{\left[\frac{d_1}{K_1} + \frac{d_2}{K_2} \right]}$$

$$K_{eq} = \frac{d}{\frac{d_1}{K_1} + \frac{d_2}{K_2}}$$

B) PARALLEL COMBINATION :-

(same dielectric ka 1 terminal +ve and dusra -ve)

$$C_{eq} = \frac{\epsilon_0}{d} [K_1 A_1 + K_2 A_2 + K_3 A_3]$$

$$K_{eq} = \frac{K_1 A_1 + K_2 A_2 + \dots}{A_1 + A_2 + \dots}$$

Introduction of dielectric b/w plates of capacitor :-

- Battery is connected :-

	Initially	Finally
Capacitance	C_0	KC_0
Potential	V_0	V_0
Charge	$Q_0 = C_0 V_0$	KQ_0
Electric field	$E_0 = V_0/d$	E_0
U_0 (Energy)	$U_0 = \frac{Q_0^2}{2C_0}$	KU_0
F_0 (Force on plate)	$F_0 = qE$	KF_0

- Battery ziddi hai V same rkhegi.

→ Battery is removed then dielectric placed.

	Initially	Finally
Capacitance	C_0	KC
Potential	$V_0 = Q_0/C_0$	V_0/K
Charge	$Q_0 = C_0 V_0$	Q_0
E. Field	$E_0 = V_0/d$	E_0/K
U_0 (Energy)	$U_0 = Q_0^2/2C_0$	U_0/K
F_0 (Force on plate)	$F_0 = qE$	F_0/K

Plate isolate hai to charge conserve rhegi