121/1 –

THE KENYA NATIONAL EXAMINATIONS COUNCIL
Kenya Certificate of Secondary Education

MATHEMATICS – Paper 1

ALT A

Nov. 2018 – 2½ hours

Name ..... Index Number .....

Candidate's Signature ..... Date .....

Instructions to candidates

(a) Write your name and index number in the spaces provided above.
(b) Sign and write the date of examination in the spaces provided above.
(c) This paper consists of **two** sections; **Section I** and **Section II**.
(d) Answer **all** the questions in **Section I** and only **five** questions from **Section II**.
(e) **Show all the steps in your calculations, giving your answers at each stage in the spaces provided below each question.**
(f) Marks may be given for correct working even if the answer is wrong.
(g) **Non-programmable** silent electronic calculators **and** KNEC Mathematical tables may be used, except where stated otherwise.
(h) **This paper consists of 18 printed pages.**
(i) **Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.**
(j) **Candidates should answer the questions in English.**

For Examiner's Use Only

Section I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Total

Section II

17	18	19	20	21	22	23	24	Total

Grand Total

SECTION I (50 marks)

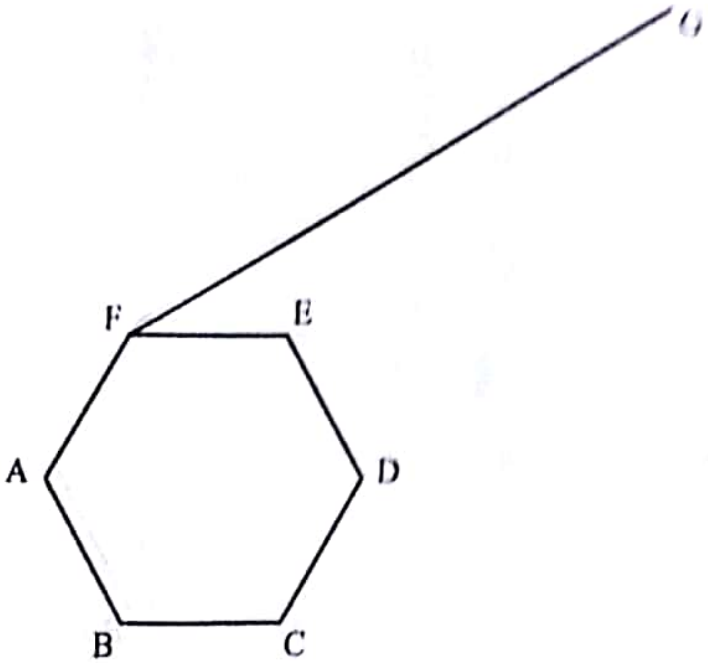
*Answer **all** the questions in this section in the spaces provided.*

1. Without using a calculator, evaluate: $\dfrac{2\frac{1}{3} - 1\frac{1}{5} \text{ of } 2}{\frac{1}{4} - \left(-\frac{1}{2}\right)^3}$ (3 marks)

2. Given that $6^{2n-3} = 7776$, find the value of n. (3 marks)

3. The base of a right pyramid is a rectangle of length 80 cm and width 60 cm. Each slant edge of the pyramid is 130 cm. Calculate the volume of the pyramid. (3 marks)

4. In the figure below ABCDEF is a uniform cross section of a solid. Given that FG is one of the visible edges of the solid, complete the sketch showing the hidden edges with broken lines.



(3 marks)

5. The lengths of three wires were 30 m, 36 m and 84 m. Pieces of wire of equal length were cut from the three wires. Calculate the least number of pieces obtained. (4 marks)

6. A two digit number is such that, the sum of its digits is 13. When the digits are interchanged, the original number is increased by 9. Find the original number. (4 marks)

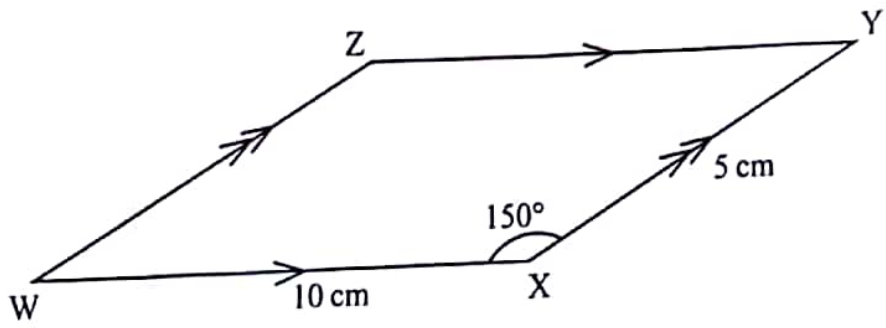
7. (a) Using a ruler and a pair of compasses only, construct a quadrilateral PQRS in which PQ = 5 cm, PS = 3 cm, QR = 4 cm, $\angle$ PQR = 135° and $\angle$ SPQ is a right angle. (2 marks)

(b) The quadrilateral PQRS represents a plot of land drawn to a scale of 1:4000. Determine the actual length of RS in metres. (2 marks)

8. Given that $\mathbf{OA} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$ and $\mathbf{OB} = \begin{pmatrix} -4 \\ 5 \end{pmatrix}$. Find the mid point M of **AB**. (2 marks)

9. Two towns R and S are 245 km apart. A bus travelling at an average speed of 60 km/h left town R for town S at 8.00 a.m. A truck left town S for town R at 9.00 a.m and met with the bus at 11.00 a.m. Determine the average speed of the truck. (4 marks)

10. In the parallelogram WXYZ below, WX = 10 cm, XY = 5 cm and ∠ WXY = 150°.



(3 marks)

Calculate the area of the parallelogram.

11. Without using mathematical tables or a calculator, evaluate $\frac{\sin 30^\circ - \sin 60^\circ}{\tan 60^\circ}$. (3 marks)

12. Use matrix method to solve: (3 marks)

$5x + 3y = 35$
$3x - 4y = -8.$

13. Expand and simplify. (2 marks)
$(2x + 1)^2 + (x - 1)(x - 3)$.

14. Use mathematical tables to find the reciprocal of 0.0247, hence evaluate (3 marks)

$\frac{\sqrt[3]{3.025}}{0.0247}$, correct to 2 decimal places.

15. A Kenyan businessman intended to buy goods worth US dollar 20000 from South Africa. Calculate the value of the goods to the nearest South Africa (S.A) Rand given that, 1 US dollar = Ksh 101.9378 and 1 S.A Rand = Ksh 7.6326. (3 marks)

16. A photograph print measuring 24 cm by 15 cm is enclosed in a frame. A uniform space of width x cm is left in between the edges of the photograph and the frame. If the area of the space is $270\,cm^2$, find the value of x. (3 marks)

SECTION II (50 marks)

*Answer any **five** questions from this section in the spaces provided.*

17. A school water tank is in the shape of a frustum of a cone. The height of the tank is 7.2 m and the top and bottom radii are 6 m and 12 m respectively.

(a) Calculate the area of the curved surface of the tank, correct to 2 decimal places. (4 marks)

(b) Find the capacity of the tank, in litres, correct to the nearest litre. (3 marks)

(c) On a certain day, the tank was filled with water. If the school has 500 students and each student uses an average of 40 litres of water per day, determine the number of days that the students would use the water. (3 marks)

18. Two vertices of a triangle ABC are A (3,6) and B (7,12).

(a) Find the equation of line AB. (3 marks)

(b) Find the equation of the perpendicular bisector of line AB. (4 marks)

(c) Given that AC is perpendicular to AB and the equation of line BC is $y = -5x + 47$, find the co-ordinates of C. (3 marks)

19. The distance covered by a moving particle through point O is given by the equation, $s = t^3 - 15t^2 + 63t - 10$.

Find:

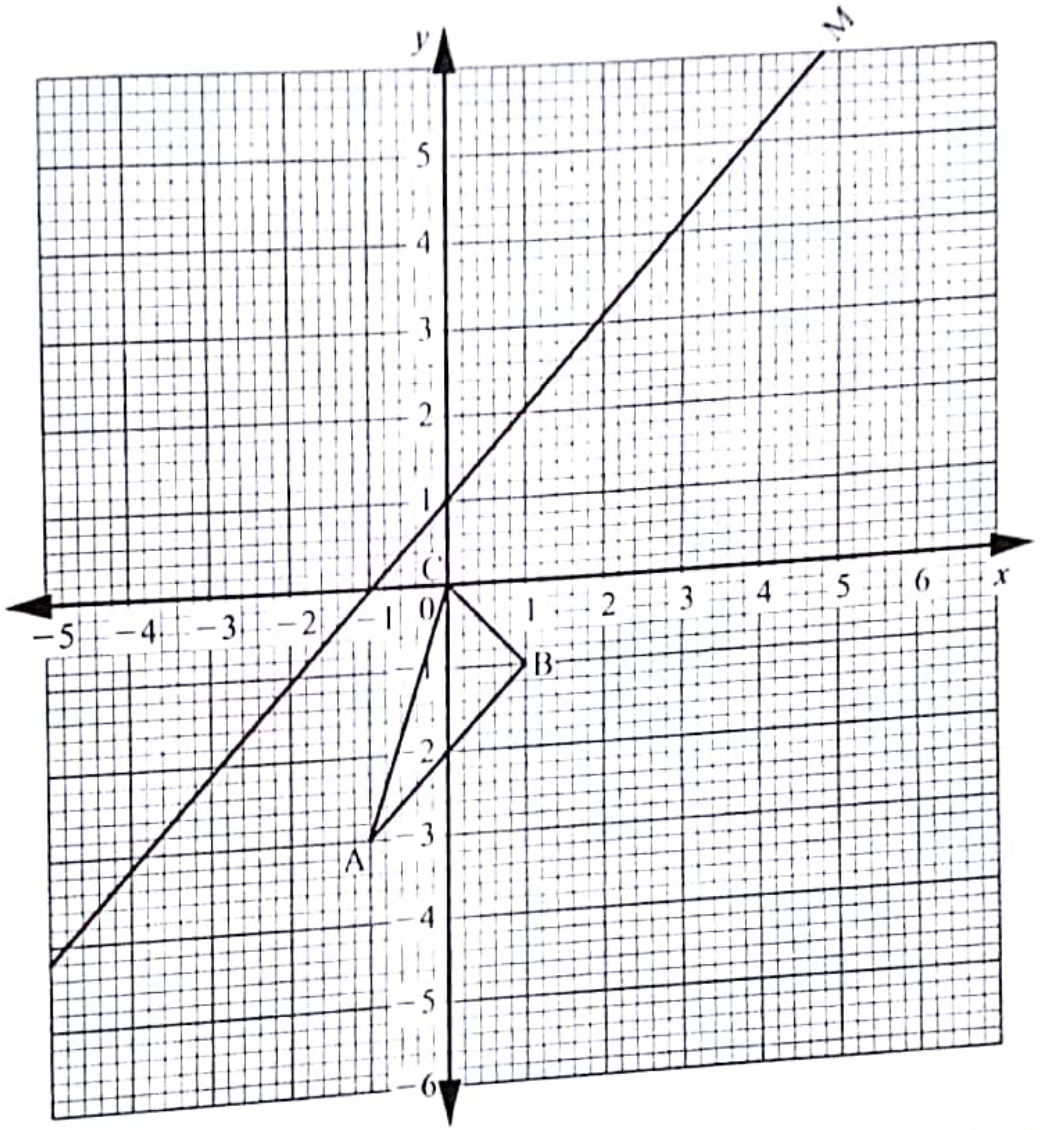
(a) distance covered when $t = 2$; (2 marks)

(b) the distance covered during the 3rd second; (3 marks)

(c) the time when the particle is momentarily at rest; (3 marks)

(d) the acceleration when $t = 5$. (2 marks)

20. The diagram below shows triangle ABC with vertices A(−1, −3), B(1, −1) and C(0,0), and line M.



(a) Draw triangle A′B′C′ the image of triangle ABC under a reflection in the line M. (2 marks)

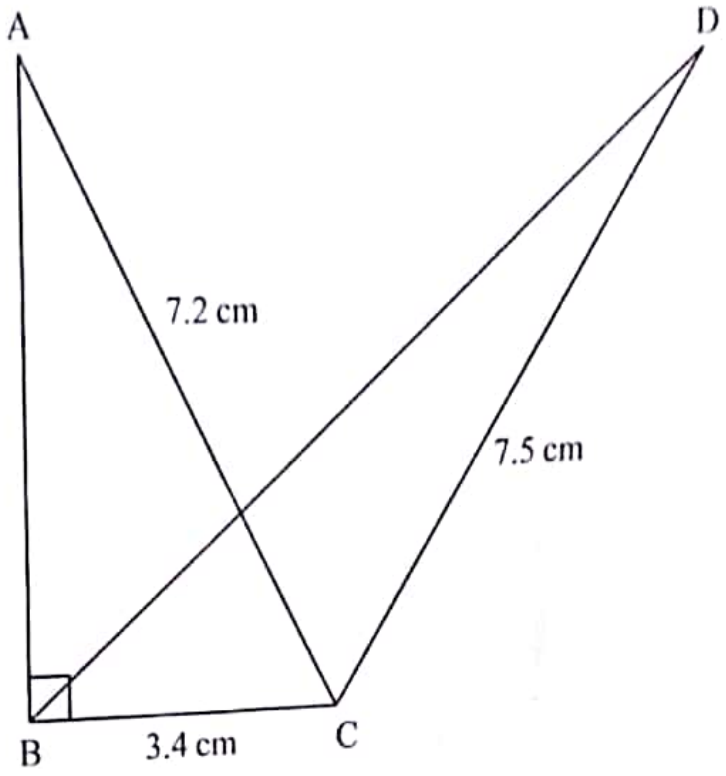
(b) Triangle A″B″C″ is the image of triangle A′B′C′ under a transformation represented by the matrix $\mathbf{T} = \begin{pmatrix} 1 & 2 \\ 0 & 1 \end{pmatrix}$

(i) Draw triangle A″B″C″ (3 marks)

(ii) Describe fully the transformation represented by matrix **T**. (3 marks)

(iii) Find the area of triangle A′B′C′ hence find area of triangle A″B″C″. (2 marks)

21. The figure below shows two triangles, ABC and BCD with a common base BC = 3.4 cm.
AC = 7.2 cm, CD = 7.5 cm and ∠ ABC = 90°.
The area of triangle ABC = Area of triangle BCD.



Calculate, correct to one decimal place: (3 marks)

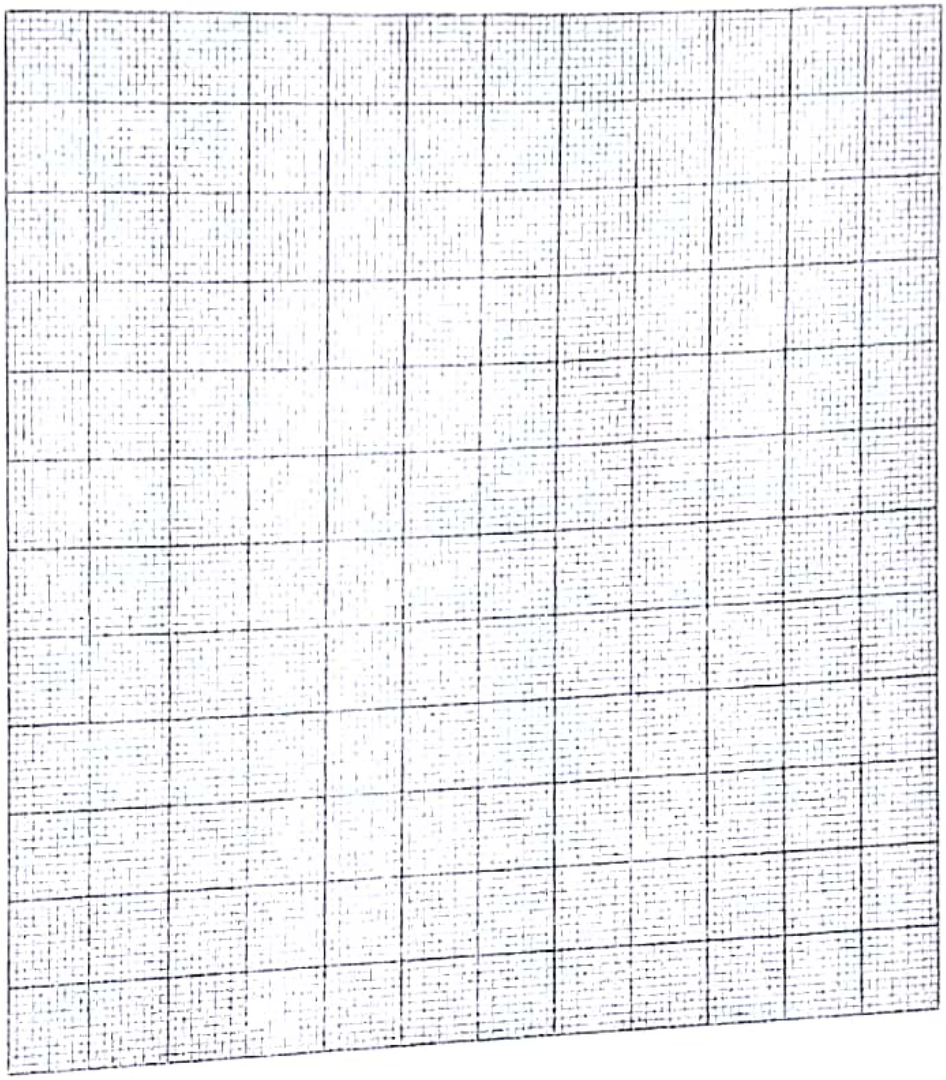
(a) the area of triangle ABC;

(b) the size of $\angle$ BCD; (3 marks)

(c) the length of BD; (2 marks)

(d) the size of $\angle$ BDC. (2 marks)

22. (a) On the grid provided, draw the graph of $y = 4 - \frac{1}{4}x^2$ for $-4 \leq x \leq 4$. (2 marks)



(b) Using trapezium rule, with 8 strips, estimate the area bounded by the curve and the x-axis. (3 marks)

(c) Find the area estimated in part (b) above by integration. (3 marks)

(d) Calculate the percentage error in estimating the area using trapezium rule. (2 marks)

23. Three business partners Abila, Bwire and Chirchir contributed Ksh 120 000, Ksh 180 000 and Ksh 240 000 respectively, to boost their business. They agreed to put 20% of the profit accrued back into the business and to use 35% of the profits for running the business (official operations). The remainder was to be shared among the business partners in the ratio of their contribution. At the end of the year, a gross profit of Ksh 225 000 was realised.

(a) Calculate the amount: (2 marks)

(i) put back into the business;

(1 mark)

(ii) used for official operations.

(4 marks)

(b) Calculate the amount of profit each partner got.

(c) If the amount put back into the business was added to individuals's shares proportionately to their initial contribution, find the amount of Chirchir's new shares. (3 marks)

24. The equation of a curve is given as $y = \frac{1}{3}x^3 - 4x + 5$. Determine:

(a) the value of y when $x = 3$; (2 marks)

(b) the gradient of the curve at $x = 3$; (3 marks)

(c) the turning points of the curve and their nature. (5 marks)

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